
Ideals, Varieties and Algorithms, *third edition*

*Errata for the **second** and subsequent printings as of November 29, 2012*

Page 15, line 2 of **Definition 1**: “ f/g and h/k ” should be “ f/g and f'/g' ”

Page 15, line 3 of **Definition 1**: “ $kh = gh$ ” should be “ $g'f = gf'$ ”

Page 27, Exercise 11.b: “part a” should be “part (a)”

Page 42, parts (i), (ii) and (iii) of **Proposition 6**: “ $\text{GCD}(f,g)$ ” should be “ $\text{GCD}(f, g)$ ” (parentheses in wrong font) (three errors)

Page 43, line 12: “ $\deg(r) > \deg(r')$ or $r = 0$ ” should be “ $\deg(r) > \deg(r')$ or $r' = 0$ ”

Page 47, line 1 of Exercise 14.b: “ $(x - a_1)^{r_1}$ ” should be “ $(x - a_1)^{r_1}$ ”

Page 52, line 1: “We rewrite the equations by subtracting the x_i terms from both sides” should be “We rewrite the equations by subtracting the x_i terms and constants from both sides”

Page 54, line -1: “Futhermore” should be “Furthermore”

Page 55, line 13: Add the sentence “A total order is also transitive, so that $x^\alpha > x^\beta$ and $x^\beta > x^\gamma$ always imply $x^\alpha > x^\gamma$.”

Page 60, line 2 of Exercise 1: “ $\text{LM}(f), \text{LT}(f)$ ” should be “ $\text{LM}(f), \text{LT}(f)$ ”

Page 62, second display: “ $-y + 1$ ” should be “ $-y + 1$ ”

Page 62, third display: The last three lines should be as follows (two errors):

$$\frac{-y + 1}{-y - 1} \\ \frac{\quad}{2}$$

Page 66, line 6: “ $\text{LT}(p) < \text{LT}(f)$ ” should be “ $\text{LT}(p) \leq \text{LT}(f)$ ”

Page 66, line 7: “ $\text{multdeg}(a_i f_i) < \text{multdeg}(f)$ ” should be “ $\text{multdeg}(a_i f_i) \leq \text{multdeg}(f)$ ”

Page 66, line 11: “30 years” should be “40 years”

Page 67, line 2: “ $\text{LT}(f_i)$ ” should be “ $\text{LT}(f_1)$ ”

Page 68, line 1 of Exercise 1: “order set” should be “ordered set”

Page 68, line 1 of Exercise 7: “ $\langle f, f_2, f_3 \rangle = \langle x^4 y^2 - z, x^4 y^2 - z, x^3 y^2 - z, x^3 y^3 - 1, x^2 y^4 - 2z \rangle$ ” should be “ $\langle f_1, f_2, f_3 \rangle = \langle x^4 y^2 - z, x^3 y^3 - 1, x^2 y^4 - 2z \rangle$ ” (multiple errors)

Page 69, Exercise 11.a: “ $\beta \in \Delta_i$, if and only if $x^{\alpha^{(i)}}$ divides x^β , but” should be “ $\beta \in \Delta_i$ if and only if $x^{\alpha^{(i)}}$ divides x^β and”

Page 72, first display: The comma at the end of the last line of the display should be a period.

Page 74, line 1 of Exercise 10: “ $k[x_1, \dots, x_n, \dots, y_1, \dots, y_n]$ ” should be “ $k[x_1, \dots, x_n, y_1, \dots, y_n]$ ”

Page 74, line 4 of Exercise 11: “ $\alpha >_{\mathbf{u}} \beta$ ” should be “ $\alpha >_{\mathbf{u}} \beta$ ”

Page 74, line 1 of Exercise 11.c: “ $u =$ ” should be “ $\mathbf{u} =$ ”

Page 76, line –8: “ $\langle \text{LT}(g_1), \dots, \text{LT}(g_t) \rangle$ ” should be “ $\langle \text{LT}(g_1), \dots, \text{LT}(g_t) \rangle$ ”

Page 77, line 1: “ $\langle \text{LT}(g_1), \dots, \text{LT}(g_t) \rangle$ ” should be “ $\langle \text{LT}(g_1), \dots, \text{LT}(g_t) \rangle$ ”

Page 77, line –7: “ $x^2 \in \langle \text{LT}(I) \rangle$ ” should be “ $x^2 \in \langle \text{LT}(I) \rangle$ ”

Page 78, line 1: “ $A_{g_1} + B_{g_2}$ ” should be “ $Ag_1 + Bg_2$ ”

Page 80, Exercise 4: “ $\text{LM}(g)$ ” should be “ $\text{LM}(g)$ ”

Page 81, line 2 of Exercise 15: “ $f_1 = f_2 = \dots 0$ ” should be “ $f_1 = f_2 = \dots = 0$ ”

Page 82, line 1 of **Corollary 2**: “ $\{g_t, \dots, g_t\}$ ” should be “ $\{g_1, \dots, g_t\}$ ”

Page 85, line 6 of proof of **Theorem 6**: “ (g_1, \dots, g_t) ” should be “ $\langle g_1, \dots, g_t \rangle$ ”

Page 88, line 2 of Exercise 10: Add the new sentence “Assume that f or g has at least two terms.”

Page 88, line 1 of Exercise 10.b: “Deduce that” should be “Deduce that $S(f, g) \neq 0$ and that”

Page 88, line 4 of Exercise 11: The numerator of right side of the equation should be “ $\text{LCM}(x^{\alpha \text{LM}(f)}, x^{\beta \text{LM}(g)})$ ”

Page 88, line 3 of Exercise 12.b: “Use part (a)” should be “Use Exercise 1”

Page 89, line 6: “Groebner basis for Γ ” should be “Groebner basis for I ”

Page 92, line 1 of **Definition 5**: “**A reduced**” should be “**A reduced**”

Page 95, line 5 of Exercise 10: “ g_i, \dots, g_t ” should be “ g_1, \dots, g_t ”

Page 95, line 1 of Exercise 10.b: “ g_i, \dots, g_t ” should be “ g_1, \dots, g_t ”

Page 97, line 3 of first display of **Example 3**: “ $2x^2-$ ” should be “ $2xy-$ ”

Page 99, line 2: “ t_i, \dots, t_m ” should be “ t_1, \dots, t_m ”

Page 103, line 5 of **Definition 1**: “ $a_1g_1 + \cdots + a_tg_t$,” should be “ $a_1g_1 + \cdots + a_tg_t$, $a_i \in k[x_1, \dots, x_n]$,”

Page 104, line 7: “ \geq ” should be “ \leq ”

Page 106, line -3: “ $\frac{x^\gamma}{\text{LM}(f_i)}\mathbf{e}_i - \frac{x^\gamma}{\text{LM}(f_j)}\mathbf{e}_j$ ” should be “ $\frac{x^\gamma}{\text{LT}(f_i)}\mathbf{e}_i - \frac{x^\gamma}{\text{LT}(f_j)}\mathbf{e}_j$ ”

Page 107, line -4: “of degree δ ” should be “of multidegree δ ”

Page 108, equation (5): “ \sum_i ” should be “ \sum_j ”

Page 108, line -3: “*Note:If*” should be “*Note: If*”

Page 109, line 1: “We leave it as an exercise to” should be “In Exercise 7, you will”

Page 110, lines 16 and 17: “we leave it as an exercise to” should be “in Exercise 9, you will”

Page 110, line -19: “that S is a” should be “that \mathcal{S} is a”

Page 110, line -9: “ S_{ik} and S_{ik} ” should be “ S_{ik} and S_{jk} ”

Page 112, line -3: “from partial” should be “from part (a).”

Page 117, line 10: “ $\text{LT}(g) \in [x_{l+1}, \dots, x_n]$ ” should be “ $\text{LT}(g) \in k[x_{l+1}, \dots, x_n]$ ”

Page 119, line 2 of the paragraph beginning “Turning”: “to x_l ” should be “to x_1 ”

Page 122, line 10: “ $\beta_i + \cdots + \beta_l$ ” should be “ $\beta_1 + \cdots + \beta_l$ ”

Page 124, **Theorem 2**: “**Theorem 2. Given**” should be “**Theorem 2 (The Geometric Extension Theorem). Given**”

Page 124, line 2 of **Theorem 2**: “ $\langle f_l, \dots, f_s \rangle$ ” should be “ $\langle f_1, \dots, f_s \rangle$ ” (two errors)

Page 128, line 7: “ $V(I_1) =$ ” should be “ $\mathbf{V}(I_1) =$ ”

Page 133, line -6: “ $g_i(t_i, \dots, t_m)x_i$ ” should be “ $g_i(t_1, \dots, t_m)x_i$ ”

Page 135, line 1 of Exercise 6.c: “only covers the” should be “only covers”

Page 136, parts (b) and (c) of Exercise 10: “part a” should be “part (a)” (two errors)

Page 136, line 3 of Exercise 11: “ $k^m - V(g)$ ” should be “ $k^m - \mathbf{V}(g)$ ”

Page 137, line 6 of Exercise 13: “ $W = V(g)$ ” should be “ $W = \mathbf{V}(g)$ ”

Page 139, line -10: “let L be line” should be “let L be the line”

Page 144, line -5: “ $1688x^2$ ” should be “ $688x^2$ ”

Page 148, Exercise 8.c: “has no singular points” should be “in \mathbb{R}^2 has no singular points when $a > 0$ ”

Page 149, line -6: “ $(0, 17.4)$ ” should be “ $(0, 17/4)$ ”

Page 150, line 1 of Exercise 20.b: “find the” should be “to find the”

Page 152, line -9: “ $d \in k[x_1, \dots, x_n]$ ” should be “ $d \in k[x_2, \dots, x_n]$ ”

Page 153, line -9: “over \mathbb{Q} ,” should be “over \mathbb{Q} .” (the comma should be a period)

Page 155, large matrix in Definition 7: There are two large braces at the bottom of the matrix. Under the right-most brace (the ones under the columns with b_i coefficients), “ m columns” should be “ l columns”

Page 157, lines 19–21: Delete these lines and replace them with the following:

“where $c_0, \dots, c_{m-1}, d_0, \dots, d_{l-1}$ are unknowns in k . Equation (6) holds if and only if substituting these formulas into (6) gives an equality of polynomials. Comparing coefficients of powers of x , we conclude that (6) is equivalent to the following system of linear equations with unknowns c_i, d_i and coefficients a_i, b_i in k .”

Page 159, line -1: “ $f_i \cdots f_r$ ” should be “ $f_1 \cdots f_r$ ”

Page 163, statement of **Proposition 1**: In two places, “ $\text{Res}(f, g, x_1)$ ” should be “ $\text{Res}(f, g, x_1)$ ” (two errors)

Page 166, line 1 of Exercise 2: “Let $f, g \in \mathbb{C}[x, y]$.” should be “Let $f, g \in \mathbb{C}[x, y]$ be nonzero.”

Page 166, line 1 of Exercise 2.b: “ $[x, y]$ ” should be “ $\mathbb{C}[x, y]$ ”

Page 166, line 1 of Exercise 3: “ $(f, g) \cap k[y]$ ” should be “ $\langle f, g \rangle \cap k[y]$ ”

Page 167, last line of Exercise 8: “Exercise 11” should be “Exercise 10”

Page 167, first display of Exercise 10.a: “ $\text{Res}(f(x_1, \mathbf{c}), g(x_1, \mathbf{c}, x_1))$ ” should be “ $\text{Res}(f(x_1, \mathbf{c}), g(x_1, \mathbf{c}), x_1)$ ”

Page 172, line -3: “ (x^n, y^m) ” should be “ $\langle x^n, y^m \rangle$ ”

Page 174, line 3 of part (a) of Exercise 7: “ a_1x^{n-1} ” should be “ $a_1x^{n-1}y$ ”

Page 180, line 1: “*the principal ideal*” should be “*be the principal ideal*”

Page 181, line -4: The left side of the equation should be “ $\frac{\partial f}{\partial x_j}$ ”

Page 183, line 3 of **Proposition 2**: “ $\langle f_1, \dots, f_r \rangle$ and $\langle g_1, \dots, g_s \rangle$ ” should be “ $\langle f_1, \dots, f_r \rangle$ and $\langle g_1, \dots, g_s \rangle$ ”

Page 184, line 2: “ $(f_1, \dots, f_r, g_1, \dots, g_s)$ ” should be “ $\langle f_1, \dots, f_r, g_1, \dots, g_s \rangle$ ”

Page 184, line 6: “ \mathbb{R}^3 ” should be “ $\mathbb{R}[x, y, z]$ ”

Page 186, line 3 of the proof of **Proposition 9**: “by any” should be “be any”

Page 192, line 2 of Exercise 13: “ $y \in K^n$ ” should be “ $y \in k^n$ ”

Page 192, line 1 of Exercise 13.b: “is an ideal” should be “is an ideal in”

Page 192, Exercise 14.d: Add a comma before “with equality”

Page 192, Exercise 15.b: Replace with “ $\alpha_A^{-1}(I' + J') \supset \alpha_A^{-1}(I') + \alpha_A^{-1}(J')$, with equality if α_A is onto.”

Page 192, Exercise 15.c: Replace “with equality if the right-hand side contains K ” with “with equality if α_A is onto and the right-hand side contains K ”

Page 193, paragraph following **Definition 2**: In three places, “ $I(\bar{S})$ ” should be “ $\mathbf{I}(\bar{S})$ ”, and in three other places, “ $I(S)$ ” should be “ $\mathbf{I}(S)$ ” (6 errors total)

Page 197, Exercise 3: “radical ideal,” should be “radical,”

Page 197, Exercise 7.a: “ $I \supset K$ where $K = \ker(\alpha_A)$ ” should be “ $I \supset \ker(\alpha_A)$ and α_A is onto”

Page 201, line 10: “ $(p \circ F) = 0$ ” should be “ $(q \circ F) = 0$ ”

Page 208, line -1: “ $W :$ ” should be “ $W =$ ”

Page 209, Exercise 5.a: “ $W = V(f)$ ” should be “ $W = \mathbf{V}(J)$ ”

Page 210, line 3 of Exercise 9: “ $(f_1 f_2 \cdots f_r)$ ” should be “ $\langle f_1 f_2 \cdots f_r \rangle$ ”

Page 220, line 5: “ $V \in \mathbb{C}^3$ ” should be “ $V \subset \mathbb{C}^3$ ”

Page 221, line 1 of Exercise 4.b: “ $\phi^{-1}(a, b)$ ” should be “ $\pi^{-1}(a, b)$ ”

Page 226, line -9: “ $[j] + [k] = J/I$ ” should be “ $[j] + [k] \in J/I$ ”

Page 229, line 2 of Exercise 10: “ (x^2) ” should be “ $\langle x^2 \rangle$ ”

Page 234, line -18: “(ii) \Rightarrow (iii)” should be “(ii) \Leftrightarrow (iii)”

Page 234, line -17: “ $g \in G$ ” should be “ $g \in G'$ ”

Page 234, line -10: “(iv) \Rightarrow (v)” should be “(iv) \Leftrightarrow (v)”

Page 236, lines -12 and -10: “Corollary 7” should be “Proposition 7” (two errors)

Page 237, Exercise 9: Replace the entire exercise with the following:

9. Suppose that $I \subset \mathbb{C}[x_1, \dots, x_n]$ is a radical ideal with a Groebner basis f_1, \dots, f_n such that $\text{LT}(f_i) = x_i^{m_i}$ for each i . Prove that $\mathbf{V}(I)$ contains *exactly* $m_1 \cdot m_2 \cdots m_n$ points.

Page 240, part (iii) of **Proposition 3**: “ $\mathbf{I}_V(V_V(J))$ ” should be “ $\mathbf{I}_V(\mathbf{V}_V(J))$ ”

Page 240, part (iv) of **Proposition 3**: “ $\mathbf{V}_V(I_V(W))$ ” should be “ $\mathbf{V}_V(\mathbf{I}_V(W))$ ”

Page 256, line 3 of Exercise 4: “ $W \subset k$ ” should be “ $W \subset \mathbb{R}$ ”

Page 256, line 4 of Exercise 4: “ $k - W$ ” should be “ $\mathbb{R} - W$ ”

Page 262, line 3: “ $\mathbf{V}(I_l) - W_1$ ” should be “ $\mathbf{V}(I_l) - W_l$ ” and in two places, “ $\pi_1(V - W_0)$ ” should be “ $\pi_l(V - W_0)$ ” (three errors total)

Page 262, line 19: “ $V'_1 \not\subset V_i$ ” should be “ $V'_1 \not\subset V'_i$ ”

Page 263, line 9: “Exercises 7” should be “Exercise 7”

Page 263, line 15: “ $\pi_1(V)$ ” should be “ $\pi_l(V)$ ”

Page 264, line 1: “ $\pi_1(V) \notin W$ ” should be “ $\pi_1(V) \not\subset \widetilde{W}$ ” (two errors)

Page 264, line 3: “ $u_r \in I_1$ ” should be “ $u_r \notin I_1$ ”

Page 274, line -6: “explicit” should be “explicit”

Page 277, line 1 of Exercise 3.a: “trigonometric” should be “trigonometric”

Page 287, line 8: “researach” should be “research”

Page 287, line 1 of Exercise 2.b: “solutons” should be “solutions”

Page 288, line 7 of Exercise 7: “for l ” should be “for I ”

Page 308, line -16: “While” should be “WHILE”

Page 321, line 7: “*elementary symmetric polynomials*” should be “*elementary symmetric functions*”

Page 326, line 1 of Exercise 13: “total degree k ” should be “total degree d ”

Page 326, line 2 of Exercise 13.a: “ $k = i_1 + 2i_2 + \cdots + ni_n$ ” should be “ $d = i_1 + 2i_2 + \cdots + ni_n$ ”

Page 329, line 4 of the proof of **Proposition 6**: “This proves (ii)” should be “This proves (i) and (ii)”

Page 334, line 1 of part (c) of Exercise 6: “ (xyz) ” should be “ $\langle xyz \rangle$ ”

Pages 338–339, proof of **Theorem 5**: The proof uses k to denote both the field and the total degree of the invariants being considered. This degree should be changed to ℓ as follows:

Changes on Page 338:

line 2: “ $\frac{1}{2}(x^2 - y^2)$ ” should be “ $\frac{1}{2}(x^2 + y^2)$ ”

line -12: “integer k ” should be “integer “ ℓ ”

line -11: “ k into” should be “ ℓ into”

line -8: “ $(x_1 + \cdots + x_n)^k$ ” should be “ $(x_1 + \cdots + x_n)^\ell$ ”

line -7: “ $|\alpha| = k$ ” should be “ $|\alpha| = \ell$ ”

line -6: The display should read “ $(x_1 + \cdots + x_n)^\ell = \sum_{|\alpha|=\ell} a_\alpha x^\alpha$ ”

line -5: “ $|\alpha| = k$ ” should be “ $|\alpha| = \ell$ ”

line -3: “ $\alpha_1 = (\alpha_1, \dots, \alpha_n)$ ” should be “ $\alpha = (\alpha_1, \dots, \alpha_n)$ ”

Changes on Page 339:

line 5: The display should read “ $(u_1 A_1 \cdot \mathbf{x} + \cdots + u_n A_n \cdot \mathbf{x})^\ell = \sum_{|\alpha|=\ell} a_\alpha (A \cdot \mathbf{x})^\alpha u^\alpha$ ”

lines 7 and 8: On the left side of this two-line display, S_k should be S_ℓ and the exponent of $(u_1 A_1 \cdot \mathbf{x} + \cdots + u_n A_n \cdot \mathbf{x})$ should be ℓ instead of k , and on the right side of the display, two of the summations should be over $|\alpha| = \ell$ instead of over $|\alpha| = k$.

line 10: This line should begin with ℓ , not k .

line 12: “ k -th power sum S_k ” should be “ ℓ -th power sum S_ℓ ”

line 14: “ $S_k = S_k$ ” should be “ $S_\ell = S_\ell$ ”

line 15: “ S_k ” should be “ S_ℓ ”

line 17: “ $S_k =$ ” should be “ $S_\ell =$ ”

line 19: The summation on the left should be over $|\alpha| = \ell$ instead of over $|\alpha| = k$.

Page 341, line 4 of the statement of **Proposition 7**: “ $k[x_1, \dots, x, y_1, \dots, y_m]$ ” should be “ $k[x_1, \dots, x_n, y_1, \dots, y_m]$ ”

Page 343, line 3 of Exercise 5.a: “ $k[f_1, \dots, x_n] \subset k[x_1, \dots, x_n]^G$ ” should be “ $k[f_1, \dots, f_m] \subset k[x_1, \dots, x_n]^G$ ”

Page 343, line 1 of Exercise 5.c: “total degree k ” should be “total degree d ”

Page 343, line 3 of Exercise 5.d: “degree k ” should be “degree d ”

Page 343, line 2 of Exercise 5.e: “total degree $< k$ ” should be “total degree $< d$ ”

Page 352, line 9: “ $J_F \cap k(x_i, \dots, x_n, y_1, \dots, y_m)$ ” should be “ $J_F \cap k[x_i, \dots, x_n, y_1, \dots, y_m]$ ”

Page 353, second display: Insert space after “if” in two places so that the display ends with:

$$= \begin{cases} 0 & \text{if } A \cdot \mathbf{a} \neq \mathbf{a} \\ f(\mathbf{a}) \neq 0 & \text{if } A \cdot \mathbf{a} = \mathbf{a} \end{cases}$$

Page 354, Exercise 2: “ $f_1, \dots, f_m \in k[x_1, \dots, x_n]$ ” should be “ $f_1, \dots, f_m \in k[x_1, \dots, x_n]$ ”

Page 361, line -11: “dividing by x” should be “dividing by x ”

Page 366, line 4 of Exercise 3.c: “part(b)” should be “part (b)”

Page 371, line 10: “ $V(x_0)$ ” should be “ $\mathbf{V}(x_0)$ ”

Page 373, line 1 of part (iv) of **Proposition 7**: “ $F(x_0, \dots, x_n)$ ” should be “ $F(x_0, \dots, x_n)$ ” (remove the extra space following F)

Page 373, line 4 of **Example 8**: “know that W” should be “know that W ”

Page 376, line 1 of Exercise 6.d: “ $U_{i_1} \cap \dots \cap U_{i_s}$ ” should be “ $U_{i_1} \cap \dots \cap U_{i_s}$ ” (two errors)

Page 376, line 2 of Exercise 6.d: “ $< i \leq n$ ” should be “ $< i_s \leq n$ ”

Page 380, line 2 of **Proposition 4**: “ $\in \mathbf{V}$ ” should be “ $\in V$ ”

Page 386, Exercise 6.b: “ $I_l \cap \dots \cap I_l$ ” should be “ $I_1 \cap \dots \cap I_l$ ”

Page 386, line 7 of Exercise 10: “ $\langle x_0, \dots, x_0 \rangle$ ” should be “ $\langle x_0, \dots, x_n \rangle$ ”

Page 386, line 2 of Exercise 11.b: “I is prime” should be “ I is prime” (wrong font)

Page 388, line -4: “ $f_j \in I,$ ” should be “ $f_j \in I.$ ” (the comma should be a period)

Page 391, line 2 of Exercise 2: “ $k[x_0, \dots, x_0]$ ” should be “ $k[x_0, \dots, x_n]$ ”

Page 392, line 2 of Exercise 7: “ $k[x_0, \dots, x_0]$ ” should be “ $k[x_0, \dots, x_n]$ ”

Page 392, line 1 of Exercise 11.b: “part a” should be “part (a)”

Page 394, line -17: “of x does” should be “of x does”

Page 394, line -4: “and y is” should be “and y is”

Page 398, line 7: “for all i” should be “for all i ”

Page 398, line 2 of **Theorem 6**: “ $\mathbf{V}(F_1, \dots, F_s) \in$ ” should be “ $\mathbf{V}(F_1, \dots, F_s) \subset$ ”

Page 403, line -7: “ $\langle f_s^h, \dots, f_s^h \rangle$ ” should be “ $\langle f_1^h, \dots, f_s^h \rangle$ ”

Page 407, line 3 of Exercise 11: “ $\{F^i : F \in I\}$ ” should be “ $\{F^{(i)} : F \in I\}$ ”

Page 412, line -8: “ $\mathbf{V}(x - z) \cap \mathbf{V}(x + z)$ ” should be “ $\mathbf{V}(x - z) \cup \mathbf{V}(x + z)$ ”

Page 415, line 18: “image of F ” should be “image of σ ”

Page 421, line 6 of Exercise 13.c: “ v_1 ” should be “ v_i ”

Page 441, line 17: “ $|J|$ denote” should be “ $|J|$ denote” (insert space)

Page 441, line -9: “ $W' = V(x_{k_1}, \dots, x_{k_s})$ “ should be “ $W' = \mathbf{V}(x_{k_1}, \dots, x_{k_s})$ ”

Page 447, line 8 of the proof of **Proposition 2**: “ $\{i_1, \dots, i_r\}$ ” should be “ $\{i_1, \dots, i_r\}$ ”

Page 448, line 14: “ $x^\alpha x_n^j \in I$ ” should be “ $x^\alpha x_n^j \notin I$ ”

Page 451, line 2: “ $T_j^s \cap T_j^s$ ” should be “ $T_i^s \cap T_j^s$ ”

Page 451, first line of first display: “ C_I ” should be “ C_1 ”

Page 451, line -19: “degree less $\leq s$ ” should be “degree $\leq s$ ”

Page 454, line -3: “ $[e_{j_1}, \dots, e_{j_r}]$ ” should be “ $[e_{j_1}, \dots, e_{j_r}]$ ”

Page 454, line -2: “ $\sum_{i \notin \{j_1, \dots, j_r\}}$ ” should be “ $\sum_{i \notin \{j_1, \dots, j_r\}}$ ”

Page 457, line -7: “subpace” should be “subspace”

Page 462, line -1: “ $HF_I(S)$ ” should be “ $HF_I(s)$ ”

Page 463, line 8 of proof of **Proposition 9**: “ $\text{LM}(f_1)$ ” should be “ $\text{LM}(f_1)$ ”

Page 463, last display: “ $HF_I(S)$ ” should be “ $HF_I(s)$ ”

Page 470, line 14: “had degree” should be “has degree”

Page 470, line 18: “Theorem 8” should be “Theorem 11”

Page 472, lines -2 and -1: “By Theorem 15 of Chapter 4, §3” should be “It is easy to show that”

Page 473, line 15: “subspace is contained” should be “subspace contained”

Page 476, line 7: “projective variety is then defined” should be “projective variety V is defined”

Page 480, line -10: “ $H - W \subset (V)$ ” should be “ $H - W \subset \pi(V)$ ”

Page 481, line -8: “the the” should be “the”

Page 489, line 4 of **Example 5**: “ $(f_1, f_2) = (x + y + z, x^2 - y^2 z^2 + z^3)$ ” should be “ $\langle f_1, f_2 \rangle = \langle x + y + z, x^2 - y^2 z^2 + z^3 \rangle$ ” (four errors)

Page 489, line 6 of **Example 5**: “ $I(C) = (f_1, f_2)$ ” should be “ $\mathbf{I}(C) = \langle f_1, f_2 \rangle$ ” (three errors)

Page 489, line 12 of **Example 5**: “rank $(J_p(f_1, f_2))$ ” should be “rank $(J_p(f_1, f_2))$ ”

Page 496, line -9: “ $f_{p,j}$ ” should be “ $f_{p,j}$ ”

Page 496, line -2: “ $f_{p,min}$ ” should be “ $f_{p,min}$ ”

Page 523, line -5: “denote $\sqrt{-1}$.” should be “denote $\sqrt{-1}$.”

Page 531, line -6: “dicussion” should be “discussion”

Page 532, line -8: “STURMFELS (1991)” should be “STURMFELS (1993)”

Page 533, line -13: “ $\text{LCMLT}(f_i, \text{LT}(f_j))$ ” should be “ $\text{LCM}(\text{LT}(f_i), \text{LT}(f_j))$ ”

Page 542, index entry for closure, projective: “386” should be “389”

Page 545, index entry for ideal, sum of: “185” should be “183”